

## 7-1 Overview

### Definition

#### ❖ Hypothesis

in statistics, is a claim or statement about a property of a population

#### Rare Event Rule for Inferential Statistics

If, under a given assumption, the probability of a particular observed event is exceptionally small, we conclude that the assumption is probably not correct.

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## 7-2 Fundamentals of Hypothesis Testing

### Null Hypothesis: $H_0$

- ❖ Statement about value of population parameter
- ❖ Must contain condition of equality
- ❖ =,  $\geq$ , or  $\leq$
- ❖ Test the Null Hypothesis **directly**
- ❖ **Reject  $H_0$  or fail to reject  $H_0$**

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### Alternative Hypothesis: $H_1$

- ❖ Must be true if  $H_0$  is false
- ❖  $\neq, <, >$
- ❖ 'opposite' of Null

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Determine the null and alternative hypothesis for the following statements:

Ex1a) The average women heights is 63.5 inches.  
 $H_0$ :  
 $H_1$ :

Ex1b) Todd scores an average of at least 20 or more points per game.  
 $H_0$ :  
 $H_1$ :

Ex1c) The mean age of a college student is less than 25 years old.  
 $H_0$ :  
 $H_1$ :

Ex1d) The mean age of a antique car in the museum is greater than 35 years old.  
 $H_0$ :  
 $H_1$ :

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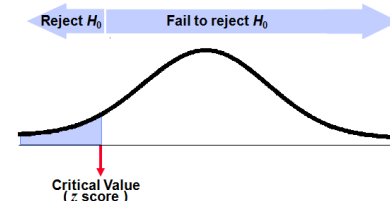
## Significance Level

- ❖ denoted by  $\alpha$
- ❖ the probability that the test statistic will fall in the critical region when the null hypothesis is actually true.
- ❖ common choices are 0.05, 0.01, and 0.10

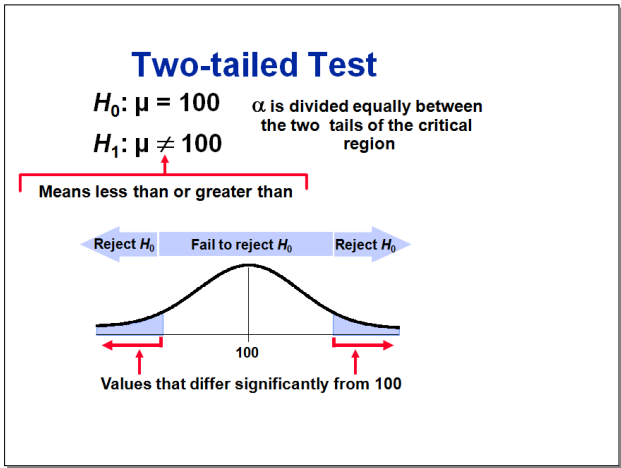
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## Critical Value

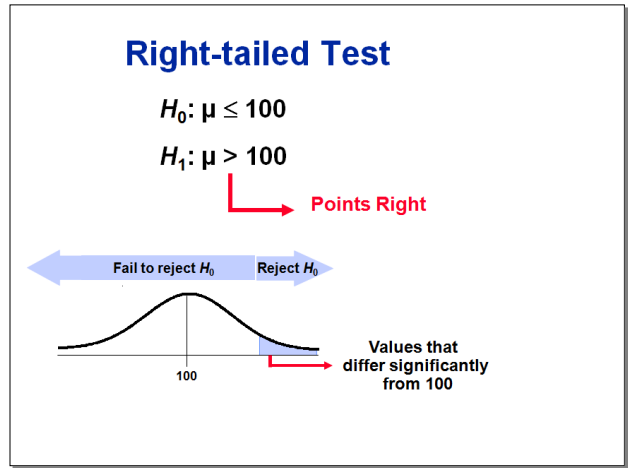
Value or values that separate the critical region (where we reject the null hypothesis) from the values of the test statistics that do **not** lead to a rejection of the null hypothesis



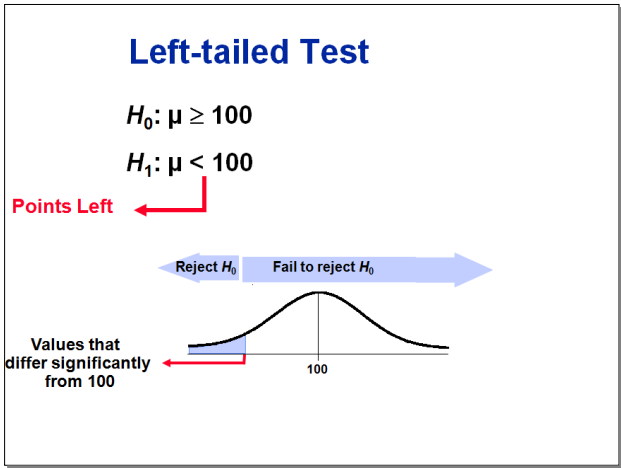
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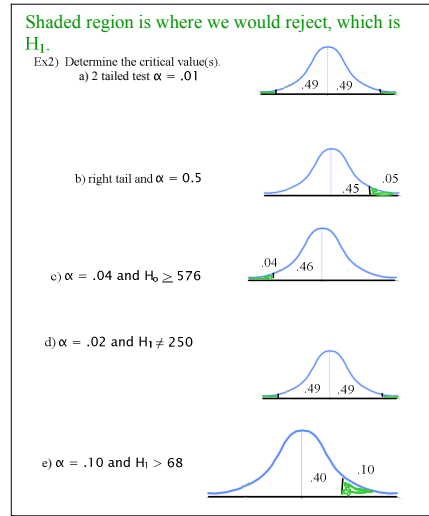
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### Test Statistic

a value computed from the sample data that is used in making the decision about the rejection of the null hypothesis

For large samples, testing claims about population means

$$z = \frac{\bar{x} - \mu_{\bar{x}}}{\frac{\sigma}{\sqrt{n}}}$$

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Ex3) Find the test statistic:  $z = \frac{\bar{x} - \mu_{\bar{x}}}{\frac{\sigma}{\sqrt{n}}}$

a) You wish to test the claim that  $\mu > 10$  at a level of significance of  $\alpha = .05$  and given  $n = 50$ ,  $\bar{x} = 10.3$ , and  $s = 1.2$ .

$$z = \frac{10.3 - 10}{\frac{1.2}{\sqrt{50}}} = 1.77$$

b) You wish to test the claim that  $\mu \leq 25$  at a level of significance of  $\alpha = .01$  and  $n = 40$ ,  $\bar{x} = 26.8$  and  $s = 4.3$ .

$$z = \frac{26.8 - 25}{\frac{4.3}{\sqrt{40}}} = 2.65$$

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## Conclusions in Hypothesis Testing

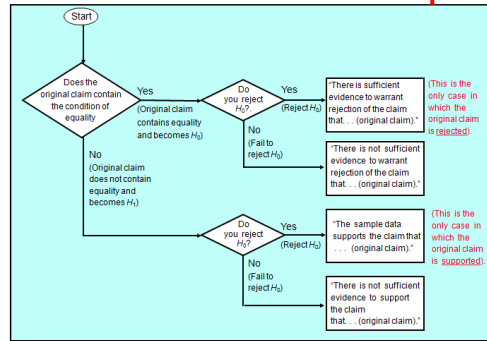
❖ always test the null hypothesis

1. **Reject** the  $H_0$
2. **Fail to reject** the  $H_0$

❖ need to formulate correct wording of final conclusion

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FIGURE 7.4 Wording of Final Conclusion p.375



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Ex4) Write a statement to reject the  $H_0$  and a statement that fails to reject the  $H_0$ .

Determine the  $H_0$  and  $H_1$  before determining your statement.

*The final statement should always include the original claim.*

- a) The Dean of a major university claims that the mean times for students to earn a Bachelor's degree is at most 5 years.

$H_0: \mu \leq 5$        $H_1: \mu > 5$

reject  $H_0$ : There is sufficient evidence to warrant rejection of the claim that the mean time to earn a Bachelor's degree is at most 5 years.

fail to reject  $H_0$ : There is not sufficient evidence to warrant rejection of the claim that the mean time to earn a Bachelor's degree is at most 5 years.

- b) The mean score for NBA games during a particular season was less than 100 points.

$H_0: \mu \geq 100$        $H_1: \mu < 100$

reject  $H_0$ : There is sufficient evidence to warrant rejection of the claim that the mean score for NBA games during a particular season was less than 100 points.

fail to reject  $H_0$ : There is not sufficient evidence to support the claim that the mean score for NBA games during a particular season was less than 100 points.

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- c) The mean grade point average of a stats students is greater than 2.9.

$H_0: \mu \leq 2.9$        $H_1: \mu > 2.9$

reject  $H_0$ : There is sufficient evidence to warrant rejection of the claim that the mean grade point average of a stats students is greater than 2.9.

fail to reject  $H_0$ : There is not sufficient evidence to support the claim that the mean grade point average of a stats students is greater than 2.9.

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## Type I Error

- ❖ The mistake of rejecting the null hypothesis when it is true.
- ❖  $\alpha$  (alpha) is used to represent the probability of a type I error
- ❖ **Example:** Rejecting a claim that the mean body temperature is 98.6 degrees when the mean really does equal 98.6

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## Type II Error

- ❖ the mistake of failing to reject the null hypothesis when it is false.
- ❖  $\beta$  (beta) is used to represent the probability of a type II error
- ❖ **Example:** Failing to reject the claim that the mean body temperature is 98.6 degrees when the mean is really different from 98.6

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Ex5) Give the type I and II errors for the following examples. It is helpful to identify the  $H_0$  and  $H_1$  first.

a) The average age for a U.S. president is 54.8 years.

$$H_0: \mu = 54.8 \quad H_1: \mu \neq 54.8$$

Type I error:

rejecting the  $H_0$ :  $\mu=54.8$ , when  $\mu = 54.8$

Type II error:

fail to reject  $H_0$ :  $\mu = 54.8$  when  $\mu \neq 54.8$

b) The mean score of an NBA basketball game is less than 100 points per game.

$$H_0: \mu \geq 100 \quad H_1: \mu < 100$$

Type I error:

rejecting  $H_0$ :  $\mu \geq 100$  when  $\mu \geq 100$

Type II error:

rejecting  $H_0$ :  $\mu \geq 100$  when  $\mu < 100$

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c) Average salary for an engineer is greater than \$66,000.

$$H_0: \mu \leq 66,000 \quad H_1: \mu > 66,000$$

Type I error:

reject  $H_0$ :  $\mu \leq 66,000$ , when  $\mu \leq 66,000$

Type II error:

failure to reject  $H_0$ :  $\mu \leq 66,000$ , when  $\mu > 66,000$

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