

Ch 6.3 Binomial Probability Distributions

Have to have the following criteria:

1. fixed number of trials
2. trials are independent
3. each trial must have all outcomes classified into 2 categories.
4. probability must remain constant.

Apr 25-8:41 AM

Determine if the examples represent a binomial probability distribution.

Ex1a) Rolling a die and keeping track of the number rolled?

Ex1b) Rolling a die and keeping track of the six's rolled?

Ex1c) Spinning a roulette wheel and keeping track of the winning number?

Ex1d) Keeping track of the number of girls born on Nov 19, 2014?

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How to find binomial probabilities

Step 1: State the distribution and the values of interest. Specify a binomial distribution with the number of trials n , success probability p , and the values of the variable clearly identified.

Step 2: Perform calculations—show your work! Do one of the following:

- (i) Use the binomial probability formula to find the desired probability; or
- (ii) use the `binompdf` or `binomcdf` command and label each of the inputs.

Step 3: Answer the question.

Nov 7-10:22 AM

Ex2a) 90% of the graduates at a State University apply to medical school are admitted. This year 6 applied. Find the p (that 4 will be accepted).

#ways it can happen $\times p(\text{happens}) \times p(\text{doesn't happen})$

formula: ${}_nC_x \cdot p^x \cdot q^{n-x}$



$${}_6C_4 \times .90^4 \times .10^2$$

$$.0984 \text{ about } 10\%$$

Press `2ND` `DISTR` and scroll to `binompdf`.
 • On the line for `n`, enter 6.
 • On the line for `p`, enter .9.
 • On the line for `x`, enter 4.
 • Press `ENTER`. The calculator displays .0984.

There are two handy commands on the TI-83/84 and TI-89 for finding binomial probabilities: `binompdf` and `binomcdf`. The inputs for both commands are the number of trials n , the success probability p , and the values of interest for the binomial random variable X .

`binompdf` (n, p, k) computes $P(X = k)$
`binomcdf` (n, p, k) computes $P(X \leq k)$ cumulative probability function

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Ex2b) The probability a car parked out in front of its house on the street gets stolen is $1/120$. What is the probability **1 gets stolen** if there are 5 cars on the street?

#ways it can happen $\times p(\text{happens}) \times p(\text{doesn't happen})$

$${}_5C_1 \times (1/120)^1 \times (119/120)^4$$

$$=.0403 \text{ about } 4\%$$

Ex 2c) $P(\text{none get stolen})$

$${}_5C_0 \times (1/120)^0 \times (119/120)^5$$

$$\text{or } (119/120)^5$$

$$=.9590 \text{ about } 96\%$$

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TRY:

Find the probability 8 out of 10 kids pass the exam if the probability of passing is 95%.

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Ex3b) In a shipment of 100 tires, there are 20 defects. What is the probability that if 5 are selected at random with each tire being replaced that **at most 2 are defective**?

$P(0) + P(1) + P(2)$ are defective

$P(\text{not defective}) = 80/100 = 4/5$

$$P(0) = {}_5C_0 \times (1/5)^0 \times (4/5)^5 =$$

$$P(1) = {}_5C_1 \times (1/5)^1 \times (4/5)^4 =$$

$$P(2) = {}_5C_2 \times (1/5)^2 \times (4/5)^3 = \underline{\hspace{2cm}}$$

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If I say that you need **at least** \$20 to go on the field trip, write an inequality to represent how much money you need to bring?

If I say you can have **no more** than 3 friends over, write an inequality to represent how many friends you can have over?

What symbol represents at least?

What symbol represents no more?

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Ex3a) Your taking a multiple choice test with 5 questions each having 4 possible answers. If you guess on everyone, what is the probability you'll get **at least 4 correct**?

$P(4 \text{ correct})$ or $P(5 \text{ correct})$

* add them for an or problem.

$${}_5C_4 \times (1/4)^4 \times (3/4)^1 + {}_5C_5 \times (1/4)^5 \times (3/4)^0$$

$$1/64$$

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Ex3c) In a shipment of 100 tires, there are 20 defects. What is the probability that if 5 are selected at random with each tire being replaced that **at least 1 tire is defective**?

$$P(1) + P(2) + P(3) + P(4) + P(5)$$

$$1 - (\text{no defects})^5$$

$$1 - ({}_5C_0 \times (1/5)^0 \times (4/5)^5)$$

$$.67232$$

Apr 25-11:58 AM

Try#2. 60% of American victims of health care fraud are senior citizens. If ten victims of health care fraud are randomly selected, what is the probability that at least 8 of them are senior citizens?

Try#3. 60% of American victims of health care fraud are senior citizens. If ten victims of health care fraud are randomly selected, what is the probability that at least 1 of them are senior citizens?

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