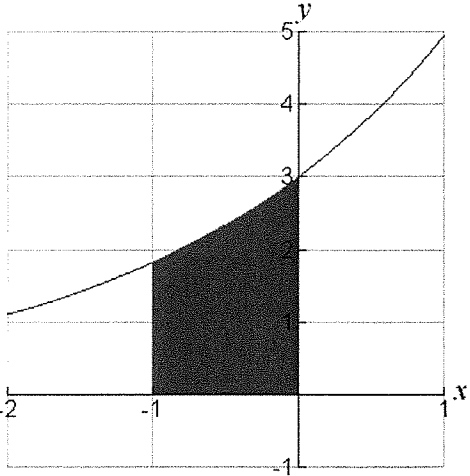


1. The functions $f(x) = 2 - x^2$ and $g(x) = -x$ are given.

<p>a. Find the area of the region bounded by the graphs of $f(x)$ and $g(x)$.</p> $\int_{-1}^2 [(2 - x^2) - (-x)] dx =$ $\int_{-1}^2 (2 - x^2 + x) dx =$ $2x - \frac{x^3}{3} + \frac{x^2}{2} \Big _{-1}^2 = \frac{9}{2}$	<p>+2: integrand</p> <p>+1: limits & answer</p>
<p>b. Find the area of the region bounded by the graph of $f(x)$ and the x-axis.</p> $\int_{-\sqrt{2}}^{\sqrt{2}} (2 - x^2) dx = 2x - \frac{x^3}{3} \Big _{-\sqrt{2}}^{\sqrt{2}}$ $= 4\sqrt{2} - \frac{4\sqrt{2}}{3}$	<p>+2: integral</p> <p>+1: answer</p>
<p>c. Find the area of the region bounded by the graph of $g(x)$, the x-axis and the line $x = 2$.</p> $\int_0^2 [0 - (-x)] dx = 2$	<p>+2: integral</p> <p>+1: answer</p>

3. $F(y) = \int_{-1}^y 3e^{x/2} dx$

<p>a. Find the accumulation function F.</p> $\int_{-1}^y 3e^{x/2} dx = 6e^{x/2} \Big _{-1}^y$ $= 6e^{y/2} - 6e^{-1/2}$	<p>+2: antiderivative</p> <p>+1: answer</p>
<p>b. Evaluate $F(-1)$, $F(0)$, and $F(4)$.</p> $F(-1) = 0$ $F(0) = 6 - 6e^{-1/2}$ $F(4) = 6e^2 - 6e^{-1/2}$	<p>+1 for 0</p> <p>+1 for $6 - 6e^{-1/2}$</p> <p>+1 for $6e^2 - 6e^{-1/2}$</p>
<p>c. Graphically show the area given by the value $F(0)$.</p> 	<p>+2: graph of $3e^{x/2}$</p> <p>+1: shaded area</p>

6. Consider the region bounded by $y = x^3$, $y = 8$, and $x = 0$.

<p>a. Find the volume of the solid formed by rotating the region about the y-axis</p> $\pi \int_0^8 (\sqrt[3]{y})^2 dy =$ $\pi \left(\frac{3}{5} y^{5/3} \right) \Big _0^8 = \frac{96}{5} \pi \approx 60.319$	<p>+2: integrand +1: limits, constant, answer</p>
<p>b. Find the volume of the solid formed by rotating the region about the x-axis.</p> $\pi \int_0^2 (8^2 - (x^3)^2) dx =$ $\pi \int_0^2 (64 - x^6) dx =$ $\pi \left[64x - \frac{x^7}{7} \right] \Big _0^2 = \frac{768}{7} \pi \approx 344.678$	<p>+2: integrand +1: limits, constant, answer</p>
<p>c. Find the volume of the solid formed by rotating the region about the line $x = 2$.</p> $\pi \int_0^8 (2^2 - (2 - \sqrt[3]{y})^2) dy =$ $\pi \int_0^8 (4y^{1/3} - y^{2/3}) dy =$ $\pi \left[3y^{4/3} - \frac{3}{5} y^{5/3} \right] \Big _0^8 =$ $\pi \left[3(16) - \frac{3}{5}(32) \right] = \frac{144}{5} \pi \approx 90.478$	<p>+2: integrand +1: limits, constant, answer</p>

7. Do the following:

<p>a. Find the distance between the points (1, 2) and (7, 10) using integration.</p> $\int_1^7 \sqrt{1 + \left(\frac{4}{3}\right)^2} dx =$ $\int_1^7 \frac{5}{3} dx = \frac{5}{3} x \Big _1^7 = 10$	<p>+2: integral +1: answer</p>
<p>b. Find the length of the curve $y = 1 + 6x^{1/2}$ on the interval $[0, 1]$.</p> $\int_0^1 \sqrt{1 + (9x^{1/2})^2} dx = \int_0^1 \sqrt{1 + 81x} dx =$ $\frac{1}{81} \left(\frac{2(1 + 81x)^{3/2}}{3} \right) \Big _0^1 = \frac{2}{243} (82^{3/2} - 1)$	<p>+2: integral +1: answer</p>
<p>c. Find the length of the curve $y = \frac{x^3}{6} + \frac{1}{2x}, \frac{1}{2} \leq x \leq 1$</p> $\int_{1/2}^1 \sqrt{1 + \left(\frac{x^2}{2} - \frac{1}{2x^2}\right)^2} dx =$ $\int_{1/2}^1 \sqrt{\frac{x^4}{4} + \frac{1}{2} + \frac{1}{4x^4}} dx = \int_{1/2}^1 \sqrt{\left(\frac{x^2}{2} + \frac{1}{2x^2}\right)^2} dx =$ $\left(\frac{x^3}{6} - \frac{1}{2x} \right) \Big _{1/2}^1 = \frac{31}{48}$	<p>+2: integral +1: answer</p>

9. Let R be the region bounded by the graph of $y = x^2 - 1$ and the graph of $x = y^2$.

$x^2 - 1 = \pm\sqrt{x}$ when $x = 0.52489$ and 1.49022 . Let $A = 0.52489$ and $B = 1.49022$.

Let $S = -\sqrt{A} = -0.72449$ and $T = \sqrt{1.49022} = 1.22074$

<p>a. Find the area of R.</p> $\text{Area} = \int_S^T (\sqrt{y+1} - y^2) dy = 1.377$	<p>+1: integrand +1: limits +1: answer</p>
<p>b. Find the volume of the solid generated when R is rotated about the vertical line $x = 2$.</p> $V = \pi \int_S^T \left((2 - y^2)^2 - (2 - \sqrt{y+1})^2 \right) dy = 11.501$	<p>+2: integrand +1: limits, constant, answer</p>
<p>c. Write, but do not evaluate, an integral expression that can be used to find the volume of the solid generated when R is rotated about the line $y = -1$.</p> <p>$V =$</p> $\pi \int_0^A \left((\sqrt{x} + 1)^2 - (-\sqrt{x} + 1)^2 \right) dx + \pi \int_A^B \left((\sqrt{x} + 1)^2 - (x^2)^2 \right) dx$	<p>+2: integrand +1: limits & constant</p>