

Calculator Problems

23. Evaluate with your calculator $y'(7.6)$, given $y = 3x^2 \ln x$.

$$115.284$$

24. Use your calculator to find $f'\left(\frac{\pi}{5}\right)$, given $f(t) = 5 \tan(x) + \sin^3(x^2)$.

$$8.154$$

25. Find the equation of the tangent line to the graph of $y = \cos^2(4x)$ at $x = \frac{\pi}{10}$.

$$y - .095 = -2.351 \left(x - \frac{\pi}{10}\right)$$

26. Given $s(t) = t^2 \sin t$, $t \geq 0$, where $s(t)$ is the position of a particle in meters after t seconds of motion.

a) Find the velocity function $v(t)$.

$$v(t) = t^2 \cos t + 2t \sin t$$

b) Find the acceleration function $a(t)$.

$$a(t) = -t^2 \sin t + 2 \sin t + 4t \cos t$$

c) Evaluate $v(4)$ and $a(4)$

$$-16.513 \quad .137$$

Evaluate $v(6)$ and $a(6)$

$$31.213 \quad 32.544$$

d) What do your answers in part (c) tell you about the speed of the particle at those times

at $t = 4$ the particle is slowing down

at $t = 6$ the particle is speeding up

27. Given the position function $s(t) = -16t^2 + 14t + 525$. Time is in seconds and distance is in feet.

a) Find the average velocity from 3 seconds to 4 seconds.

$$\frac{s(4) - s(3)}{4 - 3} = -98 \text{ ft/sec}$$

b) Find the velocity at 4 seconds.

$$-114 \text{ ft/sec}$$

c) Find the velocity when the object strikes the ground.

$$t = 6.1824 \quad -183.837 \text{ ft/sec}$$